

Enter the data into your graphing calculator.

Hours Spent Studying (x)	Test Score
2	85
3	81
4	88
5	91
6	98

```
LinReg
y=ax+b
a=3.6
b=74.2
r²=.784503632
r=.8857220963
```

Line of Best Fit

$$y = 3.6x + 74.2$$

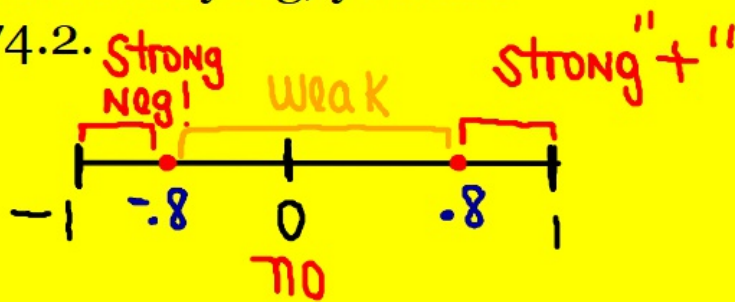
Slope = 3.6

Y-Intercept = 74.2

For every hours spent studying, your grade is predicted to increase by 3.6 points.

If you spend zero hours studying, you are predicted to earn a 74.2.

± 0.8
 ± 0.81
 ± 0.82



Plotting Data on Scatterplot

1.) Press 2nd Y=

```

2nd Y=
1:Plot1...Off
  L1 L2
2:Plot2...Off
  L1 L2
3:Plot3...Off
  L1 L2
4:PlotsOff
  
```

2.) Press Enter

```

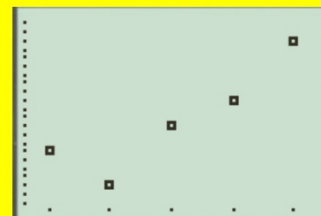
2nd Y= Plot2 Plot3
On Off
Type: [Scatter] [Line] [Bar]
      [Box-Plot] [Pie] [Histogram]
Xlist:L1
Ylist:L2
Mark: [Square] + .
  
```

3.) Press Enter to turn on Plot 1

```

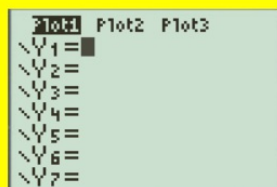
2nd Y= Plot2 Plot3
On Off
Type: [Scatter] [Line] [Bar]
      [Box-Plot] [Pie] [Histogram]
Xlist:L1
Ylist:L2
Mark: [Square] + .
  
```

4.) Press Zoom 9:
ZoomStat

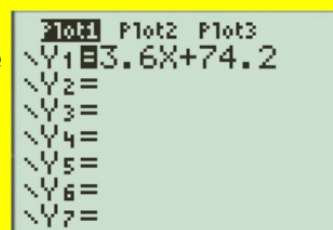


Displaying the Line of Best Fit

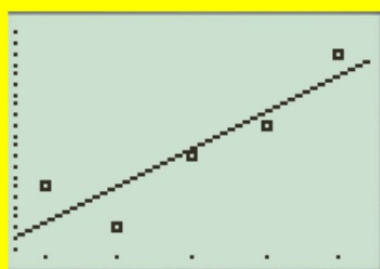
5.) Press Y=

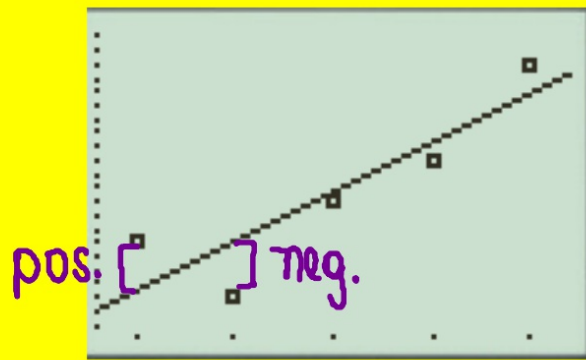


6.) Press VARS--> 5: Statistics--> EQ--> 1:RegEq--> Enter



7.) Press Graph

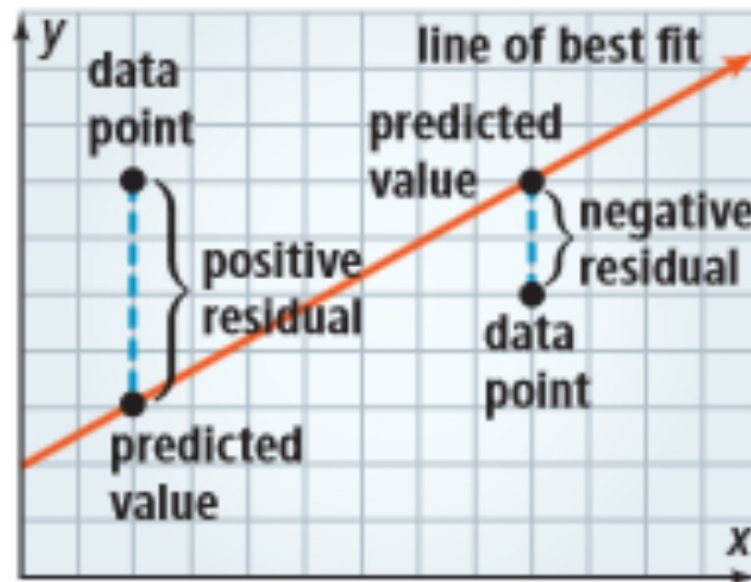




Do the actual values measure perfectly to the predicated values (line of best fit)?

NO! The distance between the line of best fit and the actual values is called a **residual**.

Residual = actual value - predicted value



Residual - Vertical distance from actual value to predicted value.

$(2, 85)$

$$y = 3.6x + 74.2$$

$$y = 3.6(2) + 74.2$$

$$y = 81.4$$

$$\begin{array}{ccccc} & 85 & - & 81.4 & = & 3.6 \\ & \downarrow & & \downarrow & & \downarrow \\ & \text{actual} & & \text{predicted} & & \text{Residual!} \end{array}$$

Residuals have numerical values!

STAT--> EDIT--> L3

L1	L2	3
2	85	-----
3	81	
4	88	
5	91	
6	98	
-----	-----	
L3 =		

2nd--> STAT--> 7: RESID

NAME	OPS	MATH
1:	L1	
2:	L2	
3:	L3	
4:	L4	
5:	L5	
6:	L6	
7:	RESID	

L1	L2	3
2	85	-----
3	81	
4	88	
5	91	
6	98	
-----	-----	
L3 = LRESID		

Press ENTER

L1	L2	L3	3
2	85	8.5	
3	81	-4	
4	88	-6	
5	91	-1.2	
6	98	2.2	
-----	-----	-----	

The numbers in L3 represent the residuals for the (x_1, y_1) points in L1 and L2.

Positive Residuals v. Negative Residuals

Positive Residuals = the predicted is value **less than** the actual value.

For example, using the equation $y = 3.6x + 74.2$, when $x = 2$
 $y = \underline{81.4}$.

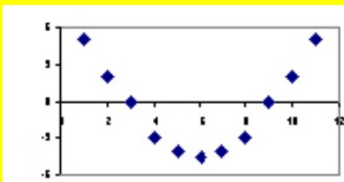
This was 3.6 units **less than** the value from the table.

Negative Residuals = the predicted value is **greater than** the actual value.

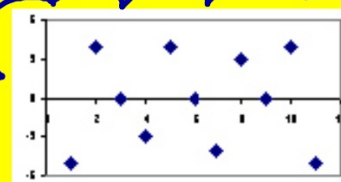
Residual Plots

A residual plot is a graph that shows the residuals on the vertical axis and the independent variable on the horizontal axis.

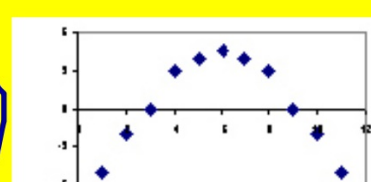
If the points in a residual plot are randomly dispersed around the horizontal axis, a linear regression model is appropriate for the data; otherwise, a non-linear model is more appropriate.



Non-random: U-shaped curve



Random pattern



Non-random: Inverted U

Ex. 1) The table shows the number of turtles that have hatched at a zoo since 2003.

	Year	Turtles Hatched
0	2003	21
1	2004	17
2	2005	16
3	2006	16
4	2007	14

A.) How many negative residuals are there? 2

B.) What is the residual value for the year 2003? 1.2

C.) Based on the line of best fit, the residual value for the year 2003 means that the predicted value is _____ the actual value.

Less than or greater than)

Ex. 2) The table below shows the number of people (in millions) who voted in U.S. Presidential elections.

Year	1980	1984	1988	1992	1996	2004
Voters	86.5	92.7	91.6	104.4	96.3	122.3

A.) How many positive residuals are there? _____

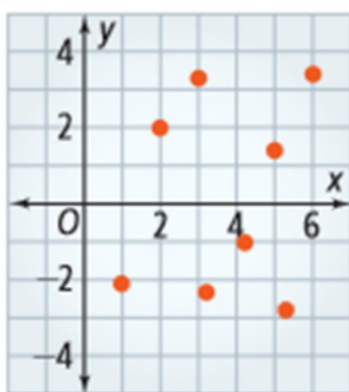
B.) What is the residual value for the year 1992? _____

C.) Based on the line of best fit, the residual value for the year 2004 means the predicted value is _____ the actual value.

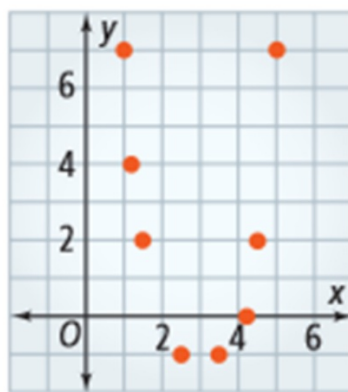
Ex. 3)

You model two data sets using linear models. The resulting residual plots are shown below. Which residual plot indicates that the linear model is a good fit for the data? Justify your answer.

Plot A



Plot B



Practice!

Complete #4, 6, and 12 on the Unit 4 Study Guide.