

1. Identify the slope from the points:

$(-2, 4)$ and $(-2, 1)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 4}{-2 - (-2)} = \frac{-3}{0} = \text{undefined}$$

2. Write the equation of a line in slope-intercept form that has a slope of $1/2$ and passes through

$(-6, 4)$.

$$m = 1/2$$

$$y = mx + b$$

$$y - y_1 = m(x - x_1)$$

$$y - 4 = \frac{1}{2}(x + 6)$$

$$y - 4 = \frac{1}{2}x + 3$$

$$\begin{array}{r} +4 \quad +4 \\ \hline y = \frac{1}{2}x + 7 \end{array}$$

3.) Write the equation of the line that passes through $(2, 3)$ and $(6, 4)$.

$$y = mx + b$$

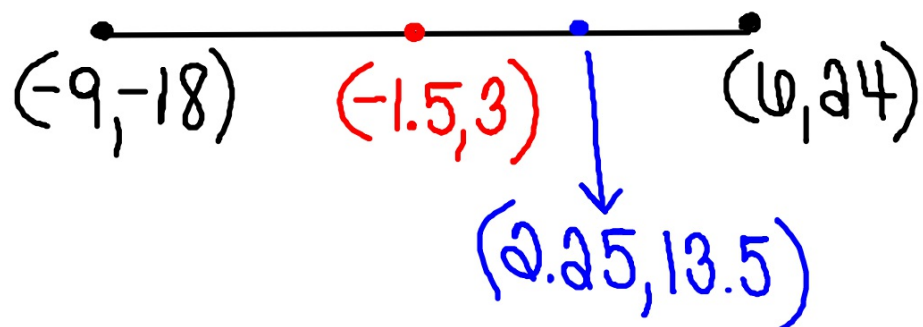
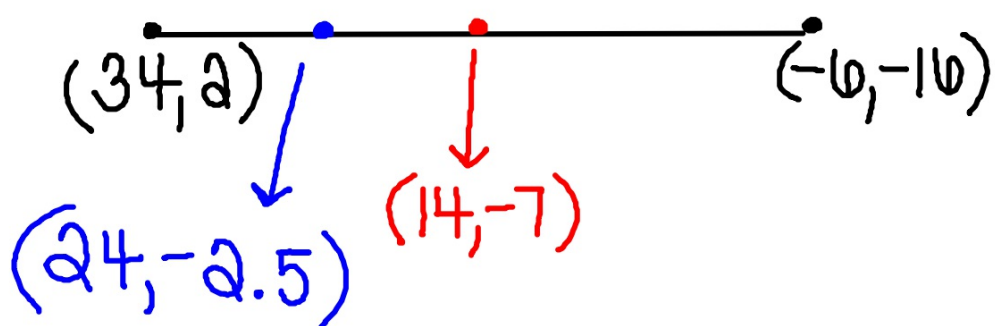
$$m = \frac{4 - 3}{6 - 2} = \frac{1}{4}$$

$$y = \frac{1}{4}x + \frac{5}{2}$$

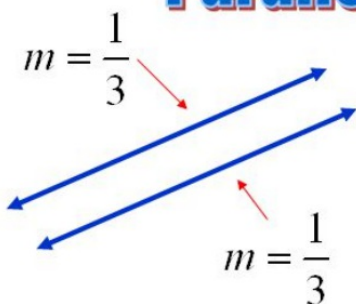
$$3 = \frac{1}{4}(2) + b$$

$$3 = \frac{1}{2} + b$$

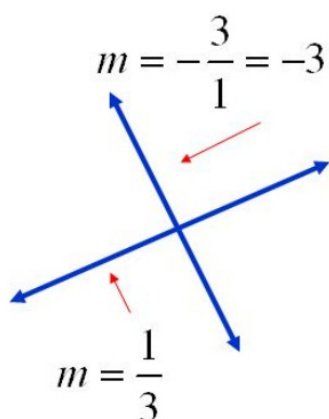
$$\begin{array}{r} 3 - \frac{1}{2} \\ \hline \frac{5}{2} = b \end{array}$$



Parallel and Perpendicular



Remember parallel lines have the same slopes so if you need the slope of a line parallel to a given line, simply find the slope of the given line and the slope you want for a parallel line will be the same.



Perpendicular lines have negative reciprocal slopes so if you need the slope of a line perpendicular to a given line, simply find the slope of the given line, take its reciprocal (flip it over) and make it negative.

$$-3 \cdot \frac{1}{3} = -\frac{3}{3} = -1$$

WRITING PARALLEL & PERPENDICULAR EQUATIONS

What is this? Given an equation, you must create ANOTHER equation that is either parallel or perpendicular to this line, passing through a certain point.

Keep in mind the following points:

- Parallel equations have equal slopes!
- Perpendicular equations have opposite Reciprocal slopes!

EXAMPLE 1:

Write the equation of the line that passes through the point $(-2, 7)$ and is **PARALLEL** to the line $y = -4x + 1$

same slope
 $m = -4$ $(-2, 7)$
 $y - y_1 = m(x - x_1)$
 $y - 7 = -4(x + 2)$
 $y - 7 = -4x - 8$
 $\begin{array}{r} +7 \qquad +7 \\ \hline y = -4x - 1 \end{array}$

Parallel Lines

EXAMPLE 2:

Write the equation of the line that passes through the point $(3, -1)$ and is **PARALLEL** to the line $x - 3y = 9$

same slope
 $x - 3y = 9$ $m = \frac{1}{3}$ $(3, -1)$
 $\begin{array}{r} x - 3y = 9 \\ -x \qquad -x \\ \hline -3y = -x + 9 \\ \frac{-3y}{-3} = \frac{-x}{-3} + \frac{9}{-3} \\ y = \frac{1}{3}x - 3 \end{array}$
 $y + 1 = \frac{1}{3}(x - 3)$
 $y + 1 = \frac{1}{3}x - 1$
 $\begin{array}{r} y + 1 = \frac{1}{3}x - 1 \\ -1 \qquad -1 \\ \hline y = \frac{1}{3}x - 2 \end{array}$

EXAMPLE 3:

Write the equation of the line that passes through the point $(4, 3)$ and is **PERPENDICULAR** to the line $y = 2x - 4$

$$m = \frac{2}{1} \perp m = -\frac{1}{2}$$

$$y - 3 = -\frac{1}{2}(x - 4)$$

$$\begin{array}{r} y - 3 = -\frac{1}{2}x + 2 \\ +3 \qquad +3 \\ \hline y = -\frac{1}{2}x + 5 \end{array}$$

Perpendicular Lines

$$y - y_1 = m(x - x_1)$$

EXAMPLE 4:

Write the equation of the line that passes through the point $(-5, 1)$ and is **PERPENDICULAR** to the line $5x + 3y = -21$

$$\begin{array}{r} 5x + 3y = -21 \\ -5x \qquad -5x \\ \hline 3y = -5x - 21 \\ \frac{3y}{3} = \frac{-5x}{3} - \frac{21}{3} \\ y = -\frac{5}{3}x - 7 \end{array}$$

$$-\frac{5}{3} \perp * \frac{3}{5}$$

$$y - 1 = \frac{3}{5}(x + 5)$$

$$\begin{array}{r} y - 1 = \frac{3}{5}x + 3 \\ +1 \qquad +1 \\ \hline \end{array}$$

$$y = \frac{3}{5}x + 4$$