

Warm Up

October 30, 2018

1.) Solve the inequality and name three solutions:

$$-2x + 7 < 17$$

2.) Find the slope: (-2, 4) and (-6, 9).

3.) Twice a number added to four is the same as one subtracted from the number? What is the number?

Write the equation of the table below.

| | | | | | | | |
|---|---|---|---|----|----|----|----|
| X | 3 | 6 | 9 | 12 | 15 | 18 | 21 |
| Y | 4 | 6 | 8 | 10 | 12 | 14 | 16 |

Unfortunately, the y-intercept cannot always be found by looking at the table.

$m = \underline{\hspace{2cm}}$

Option #1: Work Backwards

Fill in the table for $x = 0$

| | | | | | | | |
|---|---|---|---|----|----|----|----|
| X | 3 | 6 | 9 | 12 | 15 | 18 | 21 |
| Y | 4 | 6 | 8 | 10 | 12 | 14 | 16 |

Option #2: Use the Point-Slope Formula

| Main Ideas/Questions | Notes/Examples |
|--|--|
| <p>WRITING LINEAR EQUATIONS (Given a Point and Slope)</p> | <p>To write the equation of the line passing through point (x_1, y_1) with slope (m), you can use the point-slope formula:</p> <p style="text-align: center;">Point-Slope Formula:</p> <div style="text-align: center; border: 1px solid black; border-radius: 10px; height: 40px; width: 300px; margin: 0 auto;"></div> <p style="text-align: center;">*Be sure to distribute and solve for $y!$*</p> |

For tables without $x = 0$

| | | | | | | | |
|---|---|---|---|----|----|----|----|
| X | 3 | 6 | 9 | 12 | 15 | 18 | 21 |
| Y | 4 | 6 | 8 | 10 | 12 | 14 | 16 |

Writing an equation given a point and the slope.

1. (4, 1); slope = 2

2. (2, 4); slope = $\frac{1}{2}$

3. (-6, 0); slope = $\frac{2}{3}$

4. (-8, -1); slope = $-\frac{3}{4}$

1.) If x is an integer, what is the minimum value of x that satisfies the inequality?

$$\boxed{2} \quad -7(x-2) + 1 < x$$

$$-7x + 14 + 1 < x$$

$$-7x + 15 < x$$

$$+7x \quad +7x$$

$$\frac{15 < 8x}{8 \quad 8}$$

$$8x > 15$$

$$x > 1.88$$

2.) Arianna went to Marshall's and purchased a shirt for \$21.75 and socks for \$3.99. If tax was 7.5%, what was her total bill?

$$21.75 + 3.99 = 25.74$$

$$25.74 \cdot (.075) = 1.93$$

$$25.74 + 1.93 = 27.67$$

7.5% → .075

$\$27.68$

3.) Identify the slope and y-intercept:

$$2y + 5x = 16. \quad \text{Std. Form} = 5x + 2y = 16$$

$$2y + 5x = 16$$

$$-5x - 5x$$

$$\frac{2y}{2} = \frac{-5x + 16}{2}$$

$$y = -\frac{5}{2}x + 8$$

$$\boxed{m = -\frac{5}{2}}$$

$$\boxed{b = 8}$$

Writing Equations from Tables
Using Point-Slope

| # of hours | total charges |
|------------|---------------|
| +1 (1) | 145 |
| +1 (2) | 230 |
| +1 (3) | 315 |
| +1 (4) | 400 |
| +1 (5) | 485 |
| +1 (6) | 570 |

+85
+85
+85
+85
+85

$$y = mx + b$$

$$m = 85 \quad (2, 230)$$

$$y - y_1 = m(x - x_1)$$

$$y - 230 = 85(x - 2)$$

$$y - 230 = 85x - 170$$

$$+230 \qquad +230$$

$$y = 85x + 60$$

The total charges increase by \$85 every hour.
The initial fee is \$60 for zero hours worked.

Writing Equations from Tables
Using Point-Slope

| # of dogs | total charges |
|-----------|---------------|
| 1 | 65 |
| 2 | 75 |
| 3 | 85 |
| 4 | 95 |
| 5 | 105 |
| 6 | 115 |

$y = mx + b$
 $m = 10$ $(3, 85)$
 $y - 85 = 10(x - 3)$
 $y - 85 = 10x - 30$
 $+ 85$ $+ 85$

 $y = 10x + 55$

The total charges increase by \$10 for every dog.
The initial fee is \$55 for pet sitting.

What if you
are given
two points?

To write a linear equation given two points,
(x_1, y_1) and (x_2, y_2), follow this process:

Use the Slope Formula

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$



Use the Point-Slope Formula

$$y - y_1 = m(x - x_1)$$

slope
↓
↑
coordinates of a point on the line

x_1, y_1, x_2, y_2

7. (-3, 7) and (1, -1)

$$m = \frac{-1 - 7}{1 - (-3)} = \frac{-8}{4} = -2$$

$$y - 7 = -2(x - (-3))$$

$$y - 7 = -2(x + 3)$$

$$y - 7 = -2x - 6$$

$$\begin{array}{r} +7 \qquad \qquad +7 \\ \hline y = -2x + 1 \end{array}$$

8. (-6, -7) and (3, -4)

$$m = \frac{-4 - (-7)}{3 - (-6)} = \frac{3}{9} = \frac{1}{3}$$

$$y - (-7) = \frac{1}{3}(x - (-6))$$

$$y + 7 = \frac{1}{3}(x + 6)$$

$$\bullet \quad \begin{array}{r} y + 7 = \frac{1}{3}x + 2 \\ -7 \qquad \qquad -7 \end{array}$$

$$y = \frac{1}{3}x - 5$$

X_1, Y_1, X_2, Y_2

9. (2, -1) and (4, -6)

$$m = \frac{-6 - (-1)}{4 - 2} = \frac{-5}{2}$$

$$Y - (-1) = \frac{-5}{2}(X - 2)$$

$$Y + 1 = -\frac{5}{2}X + 5$$

$$Y = -\frac{5}{2}X + 4$$

X_1, Y_1, X_2, Y_2

10. (-3, -8) and (2, 7)

$$m = \frac{7 - (-8)}{2 - (-3)} = \frac{15}{5} = 3$$

$$Y - (-8) = 3(X - (-3))$$

$$Y + 8 = 3(X + 3)$$

$$Y + 8 = 3X + 9$$

$$Y = 3X + 1$$