

1. Factor
- $5x^2y - 65xy^3 + 200xy$

$$5xy(x - 13y^2 + 40)$$

2. Factor:
- $4x^3y^3 - 2x^2y^3 + 8xy^3$

$$2xy^3(2x^2 - x + 4)$$

3. Which is a binomial factor of
- $6x^2 + 3x - 14x - 7$

a.  $(6x - 1)$    b.  $(2x - 7)$    c.  $(3x + 1)$    d.  $(3x - 7)$ 

4. Clara collects dimes and nickels. She has a total of 47 coins. She counted the value of nickels and dimes and found out she has \$4.05. How many nickels,
- $n$
- , does Clara have?

$$x + y = 47$$
$$.10x + .05y = 4.05$$

$$.10x + .05(-x + 47) = 4.05$$

$$.10x - .05x + 2.35 = 4.05$$

$$.05x + 2.35 = 4.05$$

$$.05x = 1.70$$

$$x = 34 \text{ dimes}$$

$$y = 13 \text{ nickels}$$

# Factoring Trinomials

$$ax^2 + bx + c$$

## FACTORING TRINOMIALS

of the form



$$x^2 + bx + c$$

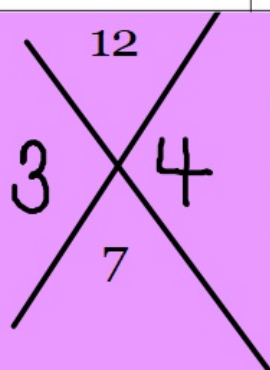
To factor a trinomial of the form  $x^2 + bx + c$ , you must find two integers that multiply to equal c and add to equal b.

Guided Example:  $x^2 + 7x + 12$   $a=1$   $b=7$   $c=12$

What two integers have a product of 12 and a sum of 7? \_\_\_\_\_

Write two binomials using these integers, then distribute to check.

$$(x+3)(x+4)$$



Top number is the product of the numbers. Bottom number is the sum.

$$\begin{array}{r|l} ac=12 & \\ \hline 1 & 12 \\ 2 & 6 \\ 3 & 4 \end{array}$$

$$\begin{array}{l} x^2 + 7x + 12 \\ (x^2 + 3x) + (4x + 12) \\ \underline{x \quad x \quad 4 \quad 4} \\ x(x+3) + 4(x+3) \\ (x+4)(x+3) \end{array}$$

## Set 1: + and +

Ex. 1) Factor  $n^2 + 9n + 20$

$$a=1 \quad b=9 \quad c=20$$

$$ac=20$$

1	20
2	10
4	5

$$\left(\frac{n^2}{n} + \frac{4n}{n}\right) + \left(\frac{5n}{5} + \frac{20}{5}\right)$$

$$n(n+4) + 5(n+4)$$

$$(n+5)(n+4)$$

Ex. 2)  $w^2 + 9w + 18$

Set 2: + and -

$$n^2 + 3n - 18$$

$$a=1 \quad b=3 \quad c=-18$$

$$ac = -18$$

-1	18
-2	9
-3	6

$$(n^2 - 3n)(+6n - 18)$$

$$n(n-3) + 6(n-3)$$

$$(n+6)(n-3)$$

$$x^2 + 2x - 8$$

What is different  
about this problem?

How will this  
impact my  
answer?

Set 3: - and -

$$a^2 - 2a - 3 \quad b = -2 \quad c = -3$$

$$ac = -3$$

-1	3
1	-3

$$(a+1)(a-3)$$

$$x^2 - 7x - 30$$

What is different  
about this problem?

How will this  
impact my  
answer?



Set 4: - and +

$$x^2 - 11x + 24$$

$$x^2 - 14x + 49$$

What is different  
about this problem?

How will this  
impact my  
answer?

WATCH THOSE SIGNS!

+ / +

$$y^2 + 2y + 1$$
$$(y + 1)(y + 1)$$

Signs are the same!  
Sign of the middle term.

- / +

$$y^2 - 2y + 1$$
$$(y - 1)(y - 1)$$

Signs are the same!  
Sign of the middle term.

- / -

$$n^2 - n - 90$$
$$(n - 10)(n + 9)$$

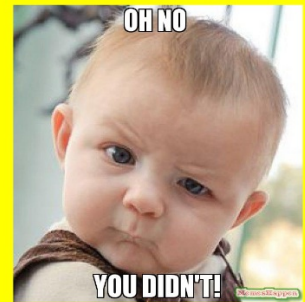
Signs are different!  
Biggest factor takes the  
sign of the middle term.

+ / -

$$m^2 + 5m - 6$$
$$(m + 6)(m - 1)$$

Signs are different!  
Biggest factor takes the  
sign of the middle term.

What if there is a GCF to factor?



$$4k^2 + 12k + 8$$

$$2x^2 - 8x - 24$$



Factor each polynomial. Check your answer by distributing.

1.)  $2x^2 + 5x + 2$

$a = 2$   $b = 5$   $c = 2$

$ac = 4$   $(2x^2 + x)(4x + 2)$

$\begin{array}{c|c} 1 & 4 \\ \hline 2 & 2 \end{array}$

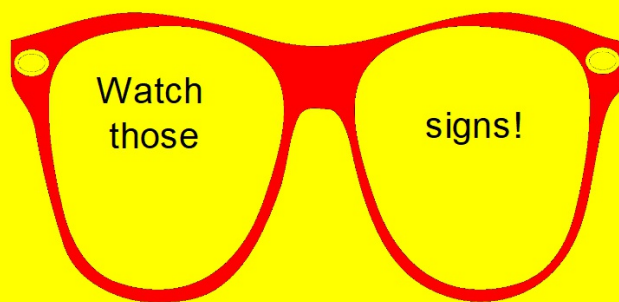
$x(2x+1) + 2(2x+1)$

$(x+2)(2x+1)$

What is different about this problem?

$$2.) 3n^2 + 5n + 2$$

$$3.) 2y^2 + 9y - 5$$



What if there is a GCF?

10.  $8x^2 - 2x - 10$

12.  $60x^2 + 4x - 8$