

## WATCH THOSE SIGNS!

+ / +

$$y^2 + 2y + 1$$
$$(y + 1)(y + 1)$$

Signs are the same!  
Sign of the middle term.

- / +

$$y^2 - 2y + 1$$
$$(y - 1)(y - 1)$$

Signs are the same!  
Sign of the middle term.

- / -

$$n^2 - n - 90$$
$$(n - 10)(n + 9)$$

Signs are different!  
Biggest factor takes the  
sign of the middle term.

+ / -

$$m^2 + 5m - 6$$
$$(m + 6)(m - 1)$$

Signs are different!  
Biggest factor takes the  
sign of the middle term.

$$2.) 3n^2 + 5n + 2$$

$$a=3 \quad b=5 \quad c=2$$

$$ac=6$$

$$\begin{array}{r|l} 1 & 6 \\ \hline 3 & 2 \end{array}$$

$$\left( \frac{3n^2}{3n} + \frac{3n}{3n} \right) \left( \frac{2n}{2} + \frac{2}{2} \right)$$

$$3n(n+1) + 2(n+1)$$

$$(3n+2)(n+1)$$

Watch  
those

signs!

$$3.) 2y^2 + 9y - 5$$

$$b^2 + 12b + 32$$

$$a=1 \quad b=12 \quad c=32$$

$$ac=32$$

$$\begin{array}{r|l} 1 & 32 \\ 2 & 16 \\ \hline 4 & 8 \end{array}$$

$$(b^2 + 4b) + (8b + 32)$$

$$b(b+4) + 8(b+4)$$


$$(b+8)(b+4)$$

## Difference of Squares

Objective: Identify and Factor Special Polynomials; Difference of Squares.

Difference of Squares:  $(a^2 - b^2)$  where  $a^2$  and  $b^2$  are perfect squares and are always separated by a subtraction sign.

## Difference of Squares

<b>WARM-UP</b>	<p><b>Directions:</b> Simplify the following polynomials.</p> <ul style="list-style-type: none"> <li>• <math>(x + 4)(x - 4) = x^2 - 4x + 4x - 16 = x^2 - 16</math></li> <li>• <math>(5m + 1)(5m - 1) = 25m^2 - 5m + 5m - 1 = 25m^2 - 1</math></li> <li>• <math>(2a + 3b)(2a - 3b) = 4a^2 - 9b^2</math></li> </ul> <p><math>4a^2 - 6ab + 6ab - 9b^2</math></p> <div style="border: 1px solid black; padding: 5px; display: inline-block;">             This resulting product is called a <b>DIFFERENCE OF SQUARES</b>.         </div> 
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<i>Steps to Factor a</i> <b>DIFFERENCE OF SQUARES</b>	<b>❶</b> First, make sure you have an actual difference of squares! (Must be a subtraction sign and you can square root both terms)
	<b>❷</b> Use the following rule to factor: $a^2 - b^2 = (a + b)(a - b)$
	<b>❸</b> Check your work by distributing!

## EXAMPLES

**Directions:** Factor each difference of squares. Check your work by distributing. If a polynomial cannot be factored, write "prime."

1.  $a^2 - 4$

$$(a+2)(a-2)$$

2.  $n^2 - 64$

$$(n+8)(n-8)$$

3.  $81 - x^2$

$$(9+x)(9-x)$$

4.  $c^2 - 100$

$$(c+10)(c-10)$$

5.  $k^2 + 25$

PRIME!

6.  $1 - 49y^2$

$$(1+7y)(1-7y)$$

7.  $9b^2 - 100$

$$(3b+10)(3b-10)$$

8.  $25x^2 - 49$

$$(5x+7)(5x-7)$$

9.  $16a^2 - 121$

10.  $x^2 - 81y^2$

11.  $4h^2 - 25g^2$

12.  $64u^2 - v^2$

Sometimes you have to take out the GCF first including variables in order to have a Difference of Squares.

Example:

$$48a^3 - 12a$$

GCF =

When you write your final answer the GCF goes outside your two ( )



**EXAMPLES  
WITH A GCF**

$$2(n+6)(n-6)$$

$$2(4s+3u)$$

$$(4s-3u)$$

**Directions:** Look for a GCF first, then factor the remaining difference of squares. Check your work by distributing.

$$21. \frac{2n^2}{2} - \frac{72}{2}$$

$$2(n^2 - 36)$$

$$22. \frac{18x^2}{2} - \frac{50}{2}$$

$$2(9x^2 - 25) \quad 2(3x+5)(3x-5)$$

$$23. \frac{32s^2}{2} - \frac{18u^2}{2}$$

$$2(16s^2 - 9u^2)$$

$$24. 45q^3 - 20q$$

$$25. 24a^2 - 54b^2$$

$$26. 100b^3 - 36b$$

$$27. 80n^4 - 125n^2$$

$$28. 8x^2y - 32y^3$$