

1.) Factor the expression:  $\frac{x^3}{x} - \frac{13x^2}{x} + \frac{42x}{x}$ .

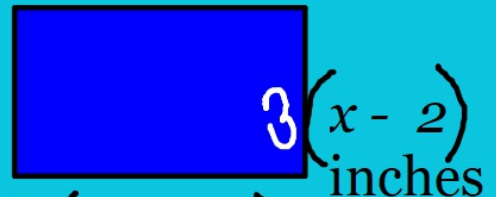
$$x(x^2 - 13x + 42)$$

$a=1 \quad b=-13 \quad c=42$

$$x(x-6)(x-7)$$

		$\cdot x$
$ac=42$		
1		42
2		21
-6		-7

2.) A rectangle has a length of  $x$  inches and a width 2 inches less than the length.



If the dimensions were 3.  $3(x \text{ inches})$  what would the area of the new rectangle be?

$$3x(3x-6) = 9x^2 - 18x \text{ units}^2$$

## Features of Quadratics

$$x = \frac{-b}{2a}$$

$$y = x^2 + 4x - 5$$

$$a=1 \quad b=4 \quad c=-5$$

Axis of Symmetry:  $x = \underline{-2}$       Vertex:  $\underline{(-2, -9)}$

$$x = \frac{-4}{2(1)} = \underline{-2}$$

$$y = (-2)^2 + 4(-2) - 5$$

Min or Max: min

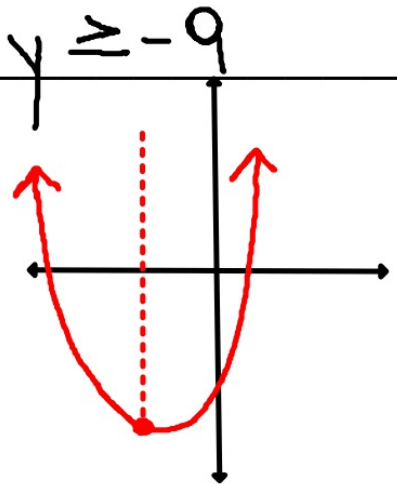
Y - Intercept:  $\underline{(0, -5)}$

$a = \text{positive}$

Domain: all real #s      Range:  $\underline{y \geq -9}$

Increasing Interval:  $\underline{x > -2}$

Decreasing Interval:  $\underline{x < -2}$



## Solving Quadratics by Graphing



### Graphing Quadratic Equations $y = ax^2 + bx + c$

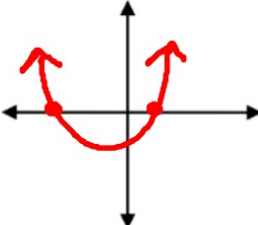
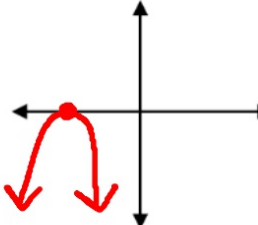
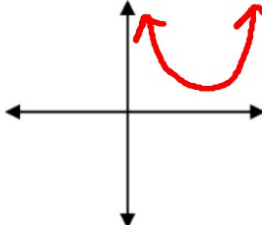
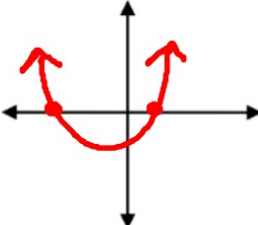
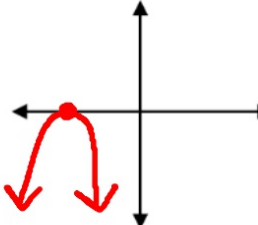
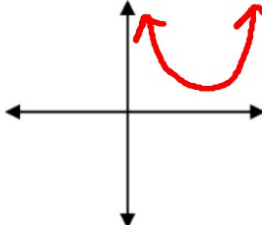
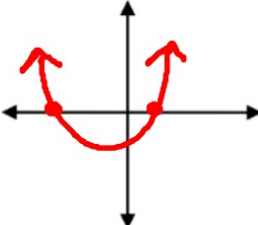
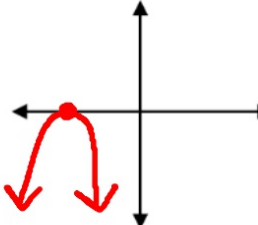
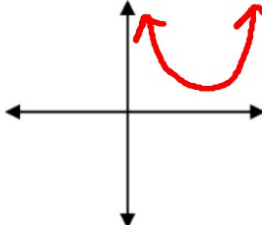
Steps to graph a quadratic equation:

- Step 1:** Find the *axis of symmetry*.
- Step 2:** Find the *vertex*.
- Step 3:** Fill in a **table of values** using your calculator.
- Step 4:** **Graph!**

To solve focus on the locations where the graph crosses the x-axis - roots, x-intercepts, zeroes.

Topic: Identifying Quadratics Roots

Date:

Main Ideas/Questions	Notes			
Definition	locations where the graph crosses the x-axis			
Also called...	solutions, x-intercepts, zeros			
Number of Solutions	<table border="0"><tr><td style="text-align: center;"><b>2 SOLUTIONS</b> </td><td style="text-align: center;"><b>1 SOLUTION</b> </td><td style="text-align: center;"><b>NO SOLUTION</b> </td></tr></table>	<b>2 SOLUTIONS</b> 	<b>1 SOLUTION</b> 	<b>NO SOLUTION</b> 
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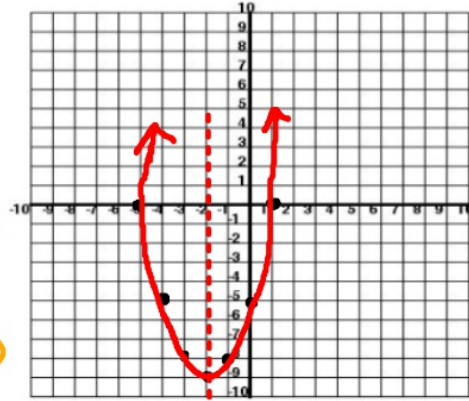
To solve focus on the locations where the graph crosses the x-axis - roots, x-intercepts, zeroes.

1.  $y = x^2 + 4x - 5$

$$X = -2$$

$$(-2, -9)$$

x	y
1	0
0	-5
-1	-4
-2	-9
-3	-10
-4	-7
-5	0



Roots:  $(-5, 0)$  and  $(1, 0)$      $( )^2 + 4( ) - 5$

- 1.) Calculate AOS:  $x = -b/2a$
- 2.) Plug AOS into original function.
- 3.) Put vertex coordinates in the center of the table.
- 4.) Fill in the table.
- 5.) Plot the points and connect the curve.
- 6.) Determine the x-intercepts.



$$2. y = x^2 - 2x + 1$$

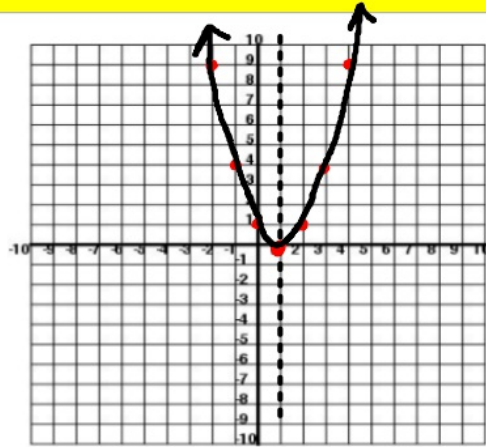
$$a=1 \quad b=-2 \quad c=1$$

$$x = \frac{-b}{2a} = 1$$

$$y = (1)^2 - 2(1) + 1$$

$$y = 0$$

x	y
1	0
0	1
2	1
3	4
4	7
5	10



Roots: (1, 0)       $( \quad )^2 - 2( \quad ) + 1$

- 1.) Calculate AOS:  $x = -b/2a$
- 2.) Plug AOS into original function.
- 3.) Put vertex coordinates in the center of the table.
- 4.) Fill in the table.
- 5.) Plot the points and connect the curve.
- 6.) Determine the x-intercepts.

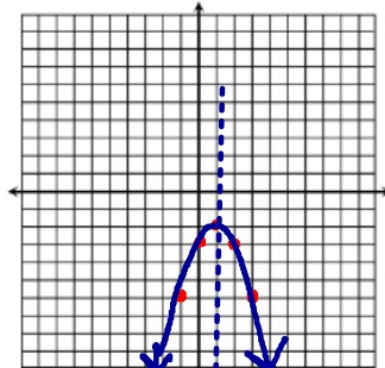
3.  $y = -x^2 + 2x - 3$

$a = -1$   $b = 2$   $c = -3$

$x = \frac{-2}{2(-1)} = 1$

$y = -(1)^2 + 2(1) - 3$

x	y
-2	-11
-1	-6
0	-3
1	-2
2	-3
3	-6
4	-11



1.) Calculate AOS:  $x = -b/2a$

no solution

2.) Plug AOS into original function.

3.) Put vertex coordinates in the center of the table.

Roots: \_\_\_\_\_

4.) Fill in the table.

5.) Plot the points and connect the curve.

6.) Determine the x-intercepts.

Roots: \_\_\_\_\_

Ex. 3) What is the equation of the graph shown?

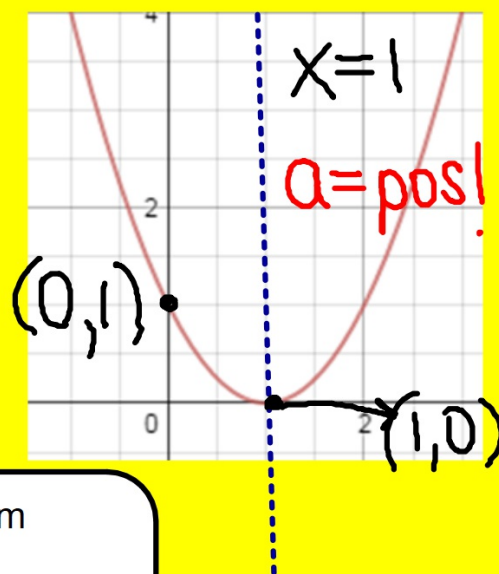
A.  ~~$y = -x^2 + 2x - 1$~~

B.  ~~$y = -x^2 - 2x - 1$~~

C.  $y = x^2 - 2x + 1$

$\frac{2}{2(1)} = 1$

D.  $y = x^2 + 2x + 1$

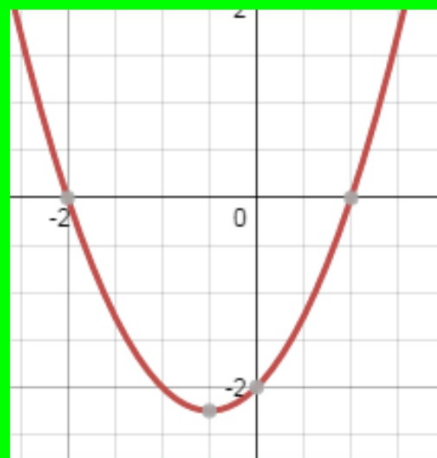


Does it have a maximum or a minimum?

Identify the AOS and vertex.



Ex. 4) What is the equation of the graph below?



A.  $y = -x^2 - 2x + 2$

B.  $y = x^2 - x - 2$

C.  $y = x^2 + x + 2$

D.  $y = x^2 + x - 2$

$$\textcircled{\#1} \frac{32a^2 - 18b^2}{2} \\ 2(16a^2 - 9b^2) \\ 2(4a+3b)(4a-3b)$$

$$\textcircled{\#18} 3x^4 + 6x^3 - 3x^2 - 6x \\ 3x(x^3 + 2x^2 - x - 2) \\ \begin{array}{l} x^2(x+2) - 1(x+2) \\ (x^2-1)(x+2) \end{array} \\ \downarrow \\ 3x(x+1)(x-1)(x+2)$$

$$\textcircled{\#19} (4y-5)^2 - 3y(4y+5) - y + 27 \\ \underline{16y^2 - 40y + 25} - \underline{12y^2 - 15y} - y + 27 \\ 4y^2 - 56y + 52 \\ 4(y^2 - 14y + 13) \\ 4(y-1)(y-13)$$