

Unit 2: Linear Functions STUDY GUIDE

1.) Select the relation that does **not** represent a function.  $\rightarrow$  *X repeats!*

- A. (18, 11), (-14, 9), (-11, 5), (2, -7)
- B. (5, 3), (-3, 9), (12, -11), (4, -3),
- C.** (5, -3), (0, -1), (9, 2), (5, -7)
- D. (-2, 10), (-3, 7), (14, 2), (3, -8)

2.) The table below displays the amount of gas used and the miles driven in a truck.

Gas Used (gallons)	Miles Driven
1	15
2	32
3	46
4	58
5	69
6	79
7	85

What is the average miles driven from 4 gallons to 7 gallons?

- A. 7 gallons
- B.** 9 gallons
- C. 13 gallons
- D. 11 gallons

$$\frac{85 - 58}{7 - 4} = \frac{27}{3}$$

3.) Leonard compared the cost of purchasing a gallon of gas at two different gas stations.

The function  $C(x) = 0.07x + 3.25$  models the average cost of a gallon of gas at the first gas station after  $x$  months. The table below shows the average cost of a gallon of gas at the second gas station after different numbers of months. Which statement is true about the two gas stations?

Numbers of Months	Cost at Second Station
2	\$3.40
4	\$3.46
6	\$3.52
8	\$3.58

*+2*  
*+2*  
*+2*

$\left. \begin{array}{l} \\ \\ \\ \end{array} \right\} +.06$

- A. The first station had a higher initial price per gallon and increased at a greater amount per month than the second station.
- B. The second station had a higher initial price per gallon and increased at a greater amount per month than the first station.
- C. The first station had a higher initial price per gallon but increased at a smaller amount per month than the second station.
- D.** The second station had a higher initial price per gallon but increased at a smaller amount per month than the first station.

$m = .03$   
 $b = 3.28$

$C(x) = .03x + 3.28$

$\hookrightarrow$  initial price

4.) Which equation is represented by the graph?

~~A.  $2x - y = 3$~~

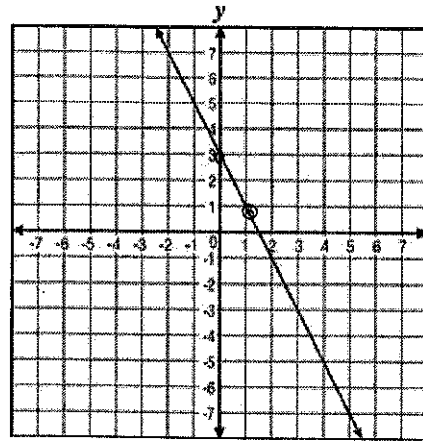
**B.  $2x + y = 3$**

C.  $2x + y = -3$

D.  $2x - y = -3$

$$\begin{array}{r} 2x - y = 3 \\ -2x \quad -2x \\ \hline -y = -2x + 3 \\ -1 \quad -1 \quad -1 \\ \hline y = 2x - 3 \end{array}$$

$$\begin{array}{r} 2x + y = 3 \\ -2x \quad -2x \\ \hline y = -2x + 3 \end{array}$$



$b = 3$   
 $m = -2$   
 $y = -2x + 3$

5.) An ordered pair is missing from the table below.

x	f(x)
-1	10
1	8
3	6
5	4
?	?

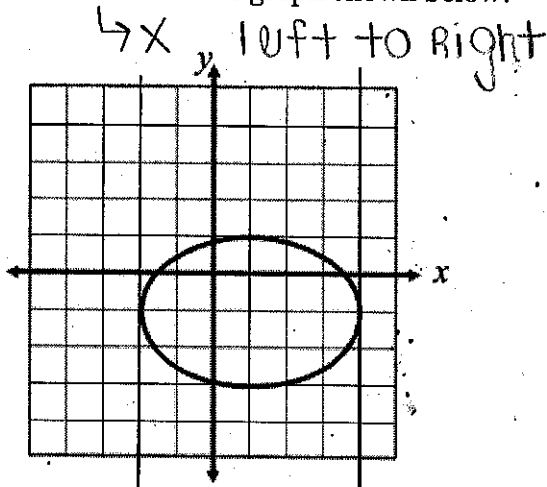
Write an ordered pair that would prevent the relation in the table from being a function. **(3, 2)**

6.) The function  $f(x) = 4x + 12$  models the yearly membership cost for a movie rental club, where  $x$  is the number of movies rented.

- Last year, Sarah rented 24 movies.  $\rightarrow 4(24) + 12 = \$108$
- Last year, Tim rented twice the amount of movies as Sarah.  $\rightarrow 4(48) + 12 = \$204$

How much more did Tim pay last year than Sarah?  
 $204 - 108 = \$96$

7.) What is the domain of the graph shown below?



**A.  $-2 \leq x \leq 4$**

~~B.  $-2 \leq y \leq 4$~~

C.  $-3 \leq x \leq 1$

~~D.  $-3 \leq y \leq 1$~~

8.) A sequence is shown below.

32, 26, 20, 14, ...

Which explicit formula can be used to determine the  $n$ th term in the sequence?

A.  $a_n = 6n + 32$

B.  $a_n = 6n + 38$

C.  $a_n = -6n + 32$

**D.  $a_n = -6n + 38$**

$a_n = d(n-1) + a_1$

$a_n = -6(n-1) + 32$   
 $= -6n + 6 + 32$

$a_n = -6n + 38$

9.) Which is the equation of the line that passes through the points  $(-4, 3)$  and  $(2, -6)$ ?

$m = \frac{-6 - 3}{2 - (-4)}$

A.  $y = -\frac{3}{2}x + 3$

~~C.  $y = \frac{3}{2}x + 3$~~

$m = \frac{-9}{6} = -\frac{3}{2}$

**B.  $y = -\frac{3}{2}x - 3$**

~~D.  $y = \frac{3}{2}x - 3$~~

$y - 3 = \frac{-3}{2}(x - (-4))$

$y - 3 = \frac{-3}{2}(x + 4)$

$y - 3 = \frac{-3}{2}x - 6$

$y = -\frac{3}{2}x - 3$

10.)

Which table of values represents a linear function? →

CONSTANT RATE OF CHANGE

x	f(x)
-3	2.75
-2	4.25
-1	6
0	7.25

x	f(x)
5	8
8	23
9	28
11	38

x	f(x)
3	14
4	15
5	13
6	14

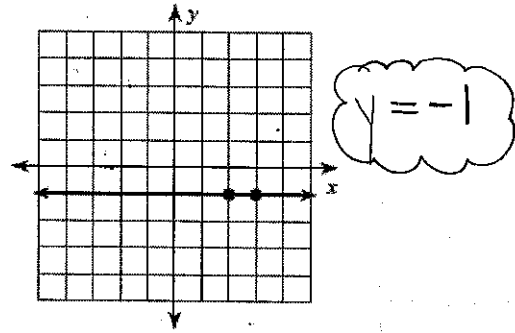
x	f(x)
-6	12
-5	10
-4	7.25
-3	5.4545

$+3$   
 $+1$   
 $+2$   
 $\frac{15}{3} = \frac{10}{2} = 5$

11.) A 4-pound bag of popcorn costs \$7.00, and a 9-pound bag of popcorn costs \$15.75. Assuming the cost of popcorn follows a linear trend, how much would a 3-pound bag of popcorn cost?

$(4, 7)(9, 15.75)$   
 $y = 1.75x$   
 $\frac{15.75 - 7}{9 - 4} = \frac{8.75}{5} = 1.75$   
 $m = 1.75$   
 $y - 7 = 1.75(x - 4)$   
 $y - 7 = 1.75x - 7$   
 $y = 1.75x$   
 $y = 1.75(3) = 5.25$

12.) Write the equation of the line graphed below.



13.) Ashtyn is saving the same amount of money each week from babysitting. After 3 weeks, she saves \$105. After 5 weeks, she saves \$165. Which equation models the amount of money Ashtyn will have saved, y, after x weeks?

$m = \frac{165 - 105}{5 - 3} = \frac{60}{2} = 30$   
 $y - 105 = 30(x - 3)$   
 $y - 105 = 30x - 90$   
 $y = 30x + 15$

14.) The graph of a linear function passes through the points (6,11) and has a slope of  $m = 3$ . Which is an equation of the function?

$y - 11 = 3(x - 6)$   
 $y - 11 = 3x - 18$   
 $y = 3x - 7$

A.  $f(x) = \frac{1}{3}x + \frac{11}{3}$   
 B.  $f(x) = \frac{1}{3}x - \frac{11}{3}$   
 C.  $f(x) = 3x - 7$   
 D.  $f(x) = 3x + 7$

15.) Write the equation of a line with a slope of -3 that passes through the point (0, -7).

A.  $y = -7x - 3$   
 B.  $y = 7x - 3$   
 C.  $y = -3x + 7$   
 D.  $y = -3x - 7$

16.) What explicit equation represents the pattern in the table below?

x	y
-4	18
-1	9
3	-3
7	-15

$+3$   
 $+4$   
 $+4$   
 $m = -3$

A.  $y = \frac{1}{3}x + 2$   
 B.  $y = -\frac{1}{3}x + 3$   
 C.  $y = 3x + 9$   
 D.  $y = -3x + 6$

17.) Jamie earns income through tips and a weekly salary. Her average weekly income can be approximated by the function  $I(x) = 10x + 150$ , where  $x$  is the number of customers she serves per week. Which statement is true?

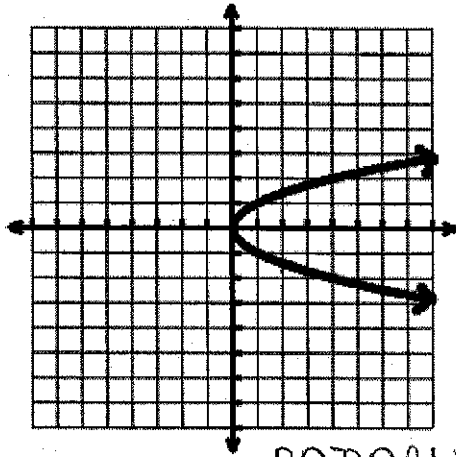
A. Jamie earns an average of \$10.00 in tips per customer she serves and is paid a weekly salary of ~~\$350~~ \$150

B. Jamie serves an average of 10 customers per week and is paid a weekly salary of \$150.

C. Jamie serves an average of 10 customers per week and earns \$150 in tips each week.

D. Jamie earns an average of \$10.00 per week and earns \$150 in tips each week.

19.) Find the range from the graph below.



RANGE:  $ARN$

21.) The function  $C(x) = 25x + 99$  models the total cost for a carpet cleaning company to clean a house, where  $x$  number of hours it takes to clean the carpet. What is the average rate of change between 2 hours and 8 hours?

\$25

18.) Use the sequence  $-7, -3, 1, 5, \dots$  to complete the following exercises:

A. Write the explicit formula:

$$a_n = 4(n-1) - 7$$

$$a_n = 4n - 4 - 7$$

$a_n = 4n - 11$

B. Write the recursive formula:

$$a_n = a_{n-1} + 4$$

C. Find  $a_{14}$ .  $4(14) - 11 = 45$

20.) What is the approximate rate of change for  $f(x) = 6x - 5$  for the interval  $-2 \leq x \leq 4$ ?

0

22.) Kaylee works at a car dealership where she earns \$300 each week in addition to 5% of her weekly sales. Write and solve a linear equation to determine what Kaylee would earn if she sold \$120,000 worth of cars this week

$$y = .05x + 300 \quad x = \text{WEEKLY SALES}$$

$$y = .05(120,000) + 300$$

$$y = 6000 + 300$$

$$y = 6300$$

23.) The function  $g(x) = 20x + 100$  model the balance of Liz's savings account after  $x$  weeks. What is the meaning of the slope in the function?

- A. The initial amount Liz starts with at the beginning of each year.
- B. The initial amount in Liz's bank account.
- C.** The additional amount Liz saves each month.
- D. The additional amount Liz saves each year.

24.) The total cost, in dollars, of membership in a basketball league is given by the function  $(m) = 35m + 60$ , where  $m$  is the number of months a person is a member. In dollars, how much is the cost of a membership for 1 year?

12 months

$$35(12) + 60$$

$$420 + 60$$

$$\boxed{\$480}$$

25.) Water is being pumped into a 10-foot tall cylindrical tank at a constant rate.

- The depth of the water is increasing linearly.
- At 1:30 pm, the water depth was 2.4 feet.
- It is now 4:00 pm, and the depth of the water is 3.9 feet.  $(1.5, 2.4)(4, 3.9)$

$$m = \frac{1.5}{2.5} = 0.6 \text{ ft per hour}$$

What will the depth (in feet) of the water be at 5:00 pm?  
 $3.9 + 0.6 = \boxed{4.5 \text{ ft}}$

26.) Two stores have movies to rent.

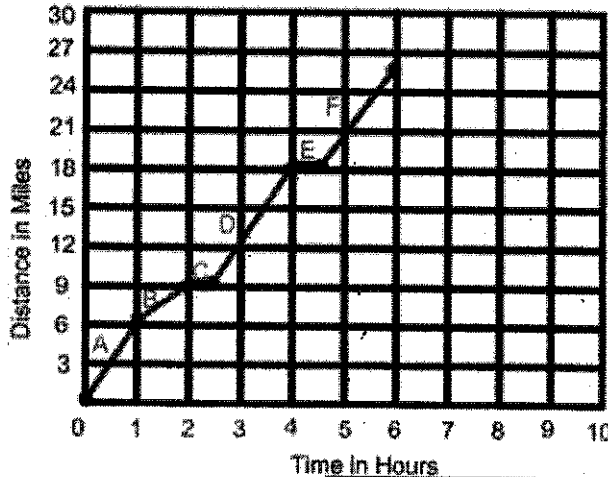
- The first store charges a \$12 per month membership fee plus \$2.50 per movie rented.  $\rightarrow 2.50x + 12$
- The second store has no membership fee but charges \$4.50 per movie rented.  $\rightarrow 4.50x$

What is the minimum number of movies a person would need to rent in a month for the first store to be a better deal?

$$\boxed{7 \text{ MOVIES}}$$

27.) The following graph represents Karen's marathon.

Karen's Marathon



During which interval did Karen have the greatest rate of change?

- A. 0 - 2 hours B. 1 - 3 hours **C.** 3 - 4 hours D. 2 - 5 hours

28.) The function  $a(n) = 3n + 2$  represents the value of the  $n$ th term in a sequence. What is the sum of the 1st and 4th terms of the sequence?

$$3(1) + 2 \quad 3(4) + 2$$

$$5 + 14 = \boxed{19}$$

29.) A function is shown below.

$$g(x) = 16.90 - 1.32x$$

What is the value of  $g(17)$ ?

$$16.90 - 1.32(17)$$

$$16.90 - 22.44$$

$$\boxed{-5.54}$$

30.) What is the slope of the line that fits this table?

X	Y
-2	-3
0	3
2	9
6	21
10	33

+2  
+2  
+4

+0  
+0  
+12

$$m = 3$$

31.) Find the fourth term of the arithmetic sequence:

$$a_1 = 7$$

$$a_n = a_{n-1} - 1.5$$

7, 5.5, 4

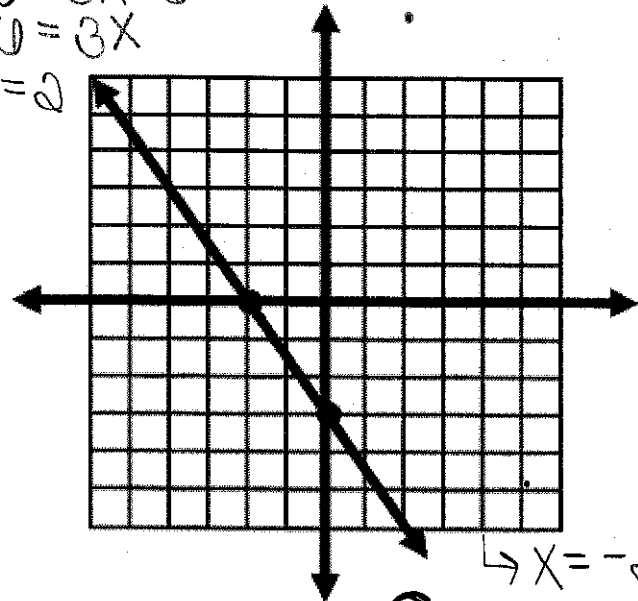
2.5  
↓  
a<sub>4</sub>

32.) Given the function  $f(x) = 3x - 6$  and the graph of the function  $g(x)$  below, determine the greatest x-intercept.

$$0 = 3x - 6$$

$$6 = 3x$$

$$x = 2$$



A. (0, -6)

C. (2, 0)

B. (-2, 0)

D. (0, -3)