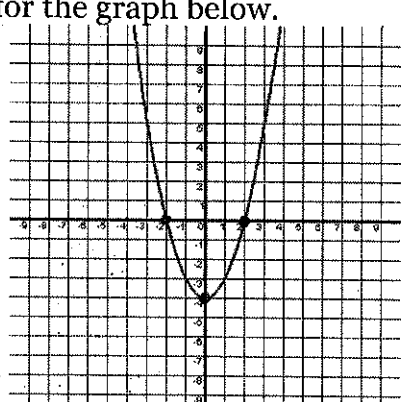


Name: _____ Block: _____ Date: _____

Unit 8: Quadratics Study Guide (HONORS -Fall 2018)

Part A: **Calculator ACTIVE.** The use of a calculator is allowed on the questions.

<p>1.) How many root(s) does the equation have? $f(x) = x^2 + 9$</p> <p>$d = b^2 - 4ac$ $= (0)^2 - 4(1)(9)$ $d = 0 - 36$ $d = -36$</p> <div style="border: 1px solid black; width: 150px; height: 50px; margin-left: 250px; text-align: center; line-height: 50px;">0</div>	<p>2.) What are the solutions of the equation? $5r^2 - 44r + 120 = -30 + 11r$</p> <p style="text-align: center;"> $\frac{-11r + 30}{5r^2 - 55r + 150} \quad \frac{+30 - 11r}{= 0}$ </p> <p>$5r^2 - 55r + 150 = 0$ $5(r^2 - 11r + 30) = 0$ $5(r - 5)(r - 6) = 0$ $5 = 0$ $r - 5 = 0$ $r - 6 = 0$ $r = 5$ $r = 6$</p> <div style="border: 1px solid black; width: 150px; height: 50px; margin-left: 250px; text-align: center; line-height: 50px;">$\{5, 6\}$</div>
<p>3.) Identify the roots to write a quadratic equation for the graph below.</p>  <p>$x = -2$ $x = 2$</p> <div style="border: 1px solid black; width: 350px; height: 50px; margin-left: 50px; padding: 5px;"> $(x + 2)(x - 2)$ $y = x^2 - 4$ </div>	<p>4.) Which expression has roots at -3 and 2?</p> <p>A. $f(x) = x^2 + x - 6$ B. $f(x) = x^2 - x - 6$ $-3, 2$ $-2, 3$</p> <p>C. $f(x) = x^2 + 3x - 2$ D. $f(x) = x^2 - 3x + 2$ $-3.5, .5$ $1, 2$</p>
<p>5.) What is the smaller of two negative consecutive integers whose product is 35?</p> <p>$n(n + 2) = 35$ $n^2 + 2n = 35$ $n^2 + 2n - 35 = 0$ $(n + 7)(n - 5) = 0$ $n + 7 = 0$ $n - 5 = 0$ $n = -7$ $n = 5$</p> <div style="border: 1px solid black; width: 150px; height: 50px; margin-left: 250px; text-align: center; line-height: 50px;">-7</div>	<p>6.) What is the minimum value of the function $f(x) = x^2 - 2x - 15$?</p> <p>$x = \frac{2}{2(1)} = 1$</p> <p>$f(x) = (1)^2 - 2(1) - 15$ $= -14$</p> <div style="border: 1px solid black; width: 150px; height: 50px; margin-left: 250px; text-align: center; line-height: 50px;">(1, -14)</div>

7.) Tonisha hit a ball into the air with an initial upward velocity of 80 feet per second. The height, $h(t)$, in feet of the ball above the ground can be modeled by $h(t) = -16t^2 + 80t + 3$ where t is the time in seconds after she hit the ball. How long does it take the ball to reach its maximum height?

$$X = \frac{-80}{2(-16)} \rightarrow \text{AOS} \quad X = 2.5 \text{ sec}$$

8.) Three times the greater of two consecutive even integers is two more than the square of the smaller. Find one of the numbers.

$$\begin{aligned} n &= 1^{\text{st}} \text{ int.} & (n-4)(n+1) &= 0 \\ n+2 &= 2^{\text{nd}} \text{ int.} & n-4 &= 0 & n+1 &= 0 \\ & & n &= 4 & n &= -1 \end{aligned}$$

$$3(n+2) = n^2 + 2$$

$$3n + 6 = n^2 + 2$$

$$-3n - 6 \quad -3n - 6$$

$$0 = n^2 - 3n - 4$$

$n = 4 \text{ OR } n = -1$

9.) What is the **sum** of the roots of the following equation?

$$f(x) = x^2 - 8x + 7$$

$$(x-1)(x-7) = 0$$

$$x-1=0 \quad x-7=0$$

$$x=1 \quad x=7$$

$\text{sum} = 8$

10.) 22. A square is altered so that one dimension is increased by 3 and the other dimension is decreased by 4. The area of the resulting rectangle is 60. Find the area of the original square.

$$(s+3)(s-4) = 60$$

$$s^2 - 4s + 3s - 12 = 60$$

$$s^2 - s - 12 = 60$$

$$s^2 - s - 72 = 0$$

$$(s-9)(s+8) = 0$$

$$s-9=0$$

$$s=9$$

$$A = s^2$$

$A = 81 \text{ units}^2$

11.) Which expression represents the solution to the equation $2x^2 + 4x - 4$?

$$X = \frac{-4 \pm \sqrt{(4)^2 - 4(2)(-4)}}{2(2)}$$

A. $1 + \sqrt{3}$ B. $-1 - \sqrt{3}$

$$X = \frac{-4 \pm \sqrt{48}}{4}$$

C. $-1 + 4\sqrt{3}$ D. $-1 - 4\sqrt{3}$

$$X = \frac{-4 \pm 4\sqrt{3}}{4}$$

$$X = -1 \pm \sqrt{3}$$

12.) Use the quadratic formula to evaluate the quadratic function below:

$$2x^2 + 9x - 15 = 0$$

$$X = \frac{-9 \pm \sqrt{(9)^2 - 4(2)(-15)}}{2(2)}$$

$$X = \frac{-9 \pm \sqrt{201}}{4}$$

$-5.79, 1.29$

13.) The discriminant of a quadratic equation is -16 . Determine the number of solutions.

NO REAL
ROOTS

14.) Use the discriminant to determine the number of solutions:

$$-3x^2 + 5x - 1$$

$$d = b^2 - 4ac$$

$$= (5)^2 - 4(-3)(-1)$$

$$d = 13$$

2
SOLUTIONS

15.) Suppose the equation $V = 40x^2 - 500x + 5000$ describes the value of a car from 1960 to 2012. What year did the car have the least value? Let 1900 be $x=0$

A. 1965
\$3500

B. 1966
\$3440

C. 1967
\$3400

D. 1968
\$3500

16.) What is the distance, in units, between the y-intercept of $g(x) = x^2 + 7x - 18$ and the y-intercept of the linear function that passes through the points shown in the table below?

x	g(x)
-5	2
10	11
25	20
60	41

y-int $g(x) = -18$

y-int table = 5

distance =
23 units

17.) Two functions are shown below.

$$f(x) = x^2 + x - 2$$

$$g(x) = -x + 1$$

Identify the point(s) at which the graphs of the two functions intersect.

(1, 0)
(-3, 4)

18.) A textile manufacturer has daily production costs of $C(x) = 10,000 - 110x + 0.045x^2$, where $C(x)$ is the total cost (in dollars) and x is the number of units produced. How many units should be produced each day to yield a minimum cost?

$$x = \frac{110}{2(0.045)}$$

$$x = 1222.22$$

1223
units

19.) The area of a rectangular lot is represented by the expression $2x^2 + x - 28$. The area of an adjacent rectangular lot is represented by the expression $2x^2 + 9x + 4$. The perimeter of the adjacent lot is 790 feet. What is the difference in the areas of the two lots?

$$\begin{aligned} &2x^2 + x - 28 \quad 2x^2 + 9x + 4 \\ &(2x^2 + 8x)(-7x - 28) \quad (2x^2 + 8x)(x + 4) \\ &2x(x + 4) - 7(x + 4) \quad 2x(x + 4) + 1(x + 4) \\ &(2x - 7)(x + 4) \quad (2x + 1)(x + 4) \\ &2(2x + 1) + 2(x + 4) \end{aligned}$$

1072

20.) Suppose the equation $h(t) = -t^2 + 5t + 14$ models the height of a ball thrown into the air off the bleachers. Which statement about the flight of the ball is true?

☒ A. The ball starts from a height of 19 feet.

☐ B. The ball takes 5 seconds to hit the ground.

☐ C. The ball takes 14 seconds to hit the ground.

☒ D. The ball reaches a maximum height of 20.25 feet.

21.) Write a quadratic equation that has an axis of symmetry at $x = -2$.

$$y = 3x^2 + 12x - 5$$

$$\begin{aligned} 14x + 2 + 2x + 8 &= 790 \\ 16x + 10 &= 790 \\ 16x &= 780 \end{aligned}$$

$x = 130$
Area
Lot 1 = 33902

Area
Lot 2 = 34974

22.) What is the larger zero of the function defined by $f(x) = x^2 - 7x - 18$?

$x = 9$

23.) A path was built through a ravine. The entrance and exit to the path are located at the x -intercepts when the path is placed on a coordinate grid. The depth of the ravine is modeled by $D(x) = 0.1x^2 + 0.1x - 11$, where x is the horizontal distance in yards. How many feet is the horizontal distance of the path?

from x -int to x -int

A. 1 foot

B. 3 feet

C. 21 feet

D. 63 feet

-11 ROOTS 10

24.) A diagram of an arched window for a model house is placed on a coordinate grid. The base of the window is on the x -axis. The arch of the window is modeled by $h(x) = -4x^2 + 10x - 6$, where x is in inches. What is the length of the base of the window?

dist between x -ints

(1,0) (1.5)

0.5 units