

Unit 9: Quadratic Equations Study Guide (INACTIVE)

Directions: Answer each question completely. You may not use a calculator.

- 1.) The function  $f(t) = -16t^2 + 96t + 112$  models the approximate height of an object  $t$  seconds after it is launched. How many seconds does it take the object to hit the ground? → ROOTS

$$\begin{aligned} -16t^2 + 96t + 112 &= 0 & -16 &= 0 \\ -16(t^2 - 6t - 7) &= 0 & t+1 &= 0 \\ -16(t-7)(t+1) &= 0 & t &= -1 \\ & & t-7 &= 0 \\ & & t &= 7 \text{ sec} \end{aligned}$$

- 2.) What is the smallest of three consecutive positive integers if the product of the smaller two integers is 4 less than 4 times the largest integer?

$$\begin{aligned} n(n+1) &= 4(n+2) - 4 \\ n^2 + n &= 4n + 8 - 4 & (n+1)(n-4) &= 0 \\ n^2 + n &= 4n + 4 & n+1 &= 0 & n-4 &= 0 \\ n^2 - 3n - 4 &= 0 & n &= -1 & n &= 4 \end{aligned}$$

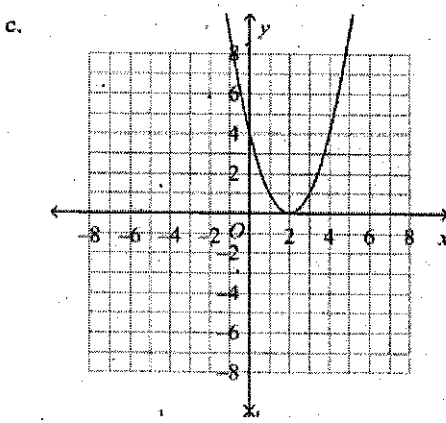
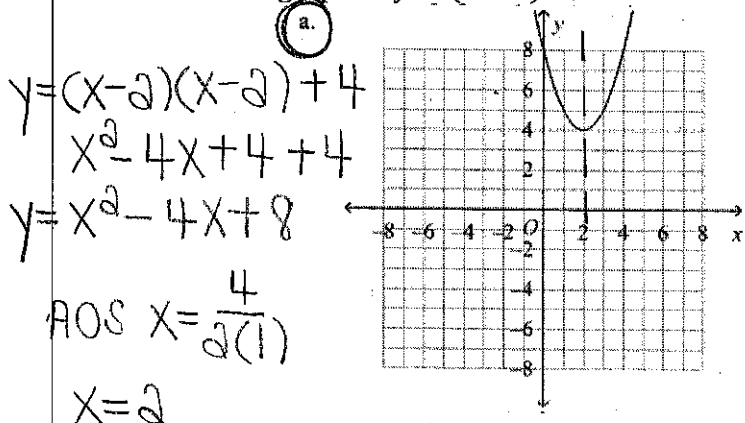
- 3.) The larger leg of a right triangle is 4 inches longer than the shorter leg. The hypotenuse is 8 inches longer than the shorter leg. Use the Pythagorean Theorem to find the length of the shorter leg.

$$\begin{aligned} (x)^2 + (x+4)^2 &= (x+8)^2 \\ x^2 + x^2 + 8x + 16 &= x^2 + 16x + 64 \\ 2x^2 + 8x + 16 &= x^2 + 16x + 64 \\ x^2 - 8x - 48 &= 0 & (x-12)(x+4) &= 0 \\ & & x &= 12 \text{ units} \end{aligned}$$

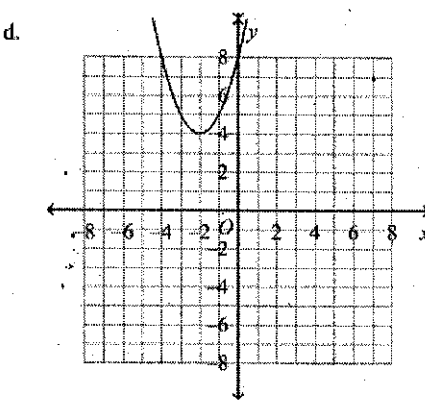
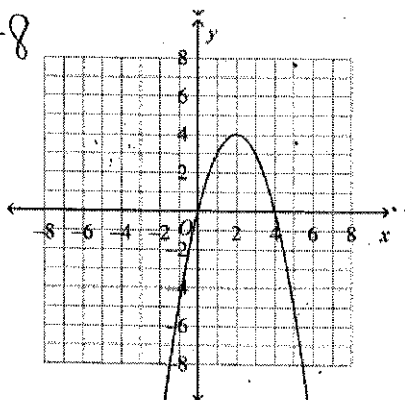
- 4.) A company models its net income, in thousands of dollars, with the function,  $p(n) = 2n^2 + 6n - 108$ , where  $x$  is the number of units of its product sold. How many units of its product does the company need to sell in order for the net income to equal \$0?

$$\begin{aligned} 2(n^2 + 3n - 54) &= 0 \\ 2(n+9)(n-6) &= 0 \\ 2=0 & n+9=0 & n-6 &= 0 \\ & n &= -9 & n &= 6 \text{ units} \end{aligned}$$

- 5.) Which is the graph of  $y = (x-2)^2 + 4$ ?



$$\begin{aligned} \text{AOS } x &= \frac{4}{2(1)} \\ x &= 2 \\ y &= (2)^2 - 4(2) + 8 \\ &= 4 - 8 + 8 \\ y &= 4 \\ (2, 4) \end{aligned}$$



6.) What is the negative root of  $y = 4x^2 - 36$ ?

$$4(x^2 - 9) = 0$$

$$4 = 0 \quad x + 3 = 0 \quad x - 3 = 0$$

$$x = -3$$

$$x = 3$$

7.) What is the value of the larger zero of

$$y = 4x^2 + 10x - 24$$

$$2(2x^2 + 5x - 12)$$

$$2(2x^2 + 8x - 3x - 12) = 0$$

$$2x(x + 4) - 3(x + 4) = 0$$

$$2(2x - 3)(x + 4) = 0$$

$$2x - 3 = 0$$

$$2x = 3$$

$$x = \frac{3}{2}$$

$$x + 4 = 0$$

$$x = -4$$

8.) Graph  $f(x) = 2x^2 + 2x - 2$ . Label the vertex and axis of symmetry.

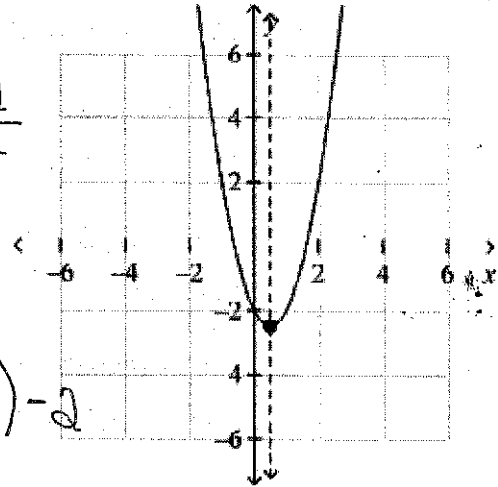
~~X~~

$$x = \frac{-2}{2(2)} = \frac{-2}{4}$$

$$x = \frac{-1}{2}$$

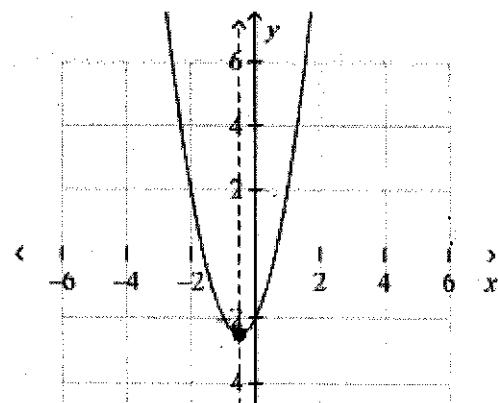
$$f(x) = 2\left(\frac{-1}{2}\right)^2 + 2\left(\frac{-1}{2}\right) - 2$$

$$f(x) = -2.5$$

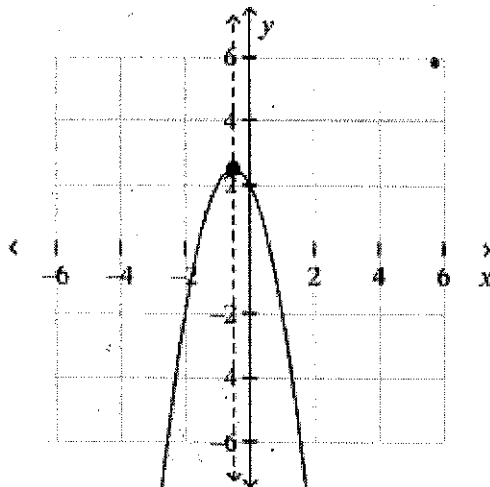


Axis of symmetry:  $x = 0.5$   
Vertex:  $(0.5, -2.5)$

(B)



~~X~~



Axis of symmetry:  $x = -0.5$   
Vertex:  $(-0.5, 2.5)$

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